

1. Solve  $5x+3=9x-7+2x$   

$$= \frac{5}{3}$$

2. Solve  $\frac{3}{x^2-3x} + \frac{4}{x} = \frac{1}{x-3}$

When you solve you get  $x=3$ , which does not check.

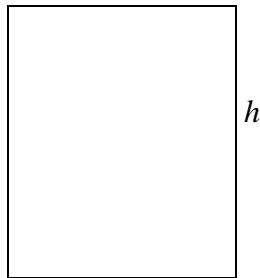
Answer: no solution

3. Solve for  $w$ :  $P = 2l + 2w$

$$w = \frac{P-2l}{2}$$

4. A picture frame has a total perimeter of 21 feet. The width is  $\frac{3}{4}$  of the height. Find the dimensions of the picture frame.

$$w = \frac{3}{4}h$$



First find the perimeter in terms of  $h$ .

$$\begin{aligned} P &= 2h + 2w \\ &= 2h + 2\left(\frac{3}{4}h\right) \\ &= 2h + \frac{3}{2}h \\ &= \frac{4}{2}h + \frac{3}{2}h = \frac{7}{2}h \end{aligned}$$

Now since we know that the perimeter is 21 feet we have

$$\begin{aligned} \frac{7}{2}h &= 21 \\ h &= \frac{2}{7}(21) \\ h &= 6 \end{aligned}$$

Then  $w = \frac{3}{4}h = \frac{3}{4}(6) = \frac{9}{2}$  Answer: Height = 6 ft, width =  $\frac{9}{2}$  ft

5. Simplify and write the result in standard form  $(11 - 5i) - (-4 + 3i)$   
 $15 - 8i$

6. Simplify and write the result in standard form  $(\frac{3}{5} - \frac{5}{6}i) + (\frac{4}{3} + \frac{1}{3}i)$   
 $\frac{29}{15} - \frac{1}{2}i$

7. Simplify and write the result in standard form  $(3 - 5i)(-2 + 4i)$   
 $14 + 22i$

8. Simplify and write the result in standard form  $\frac{2 - 5i}{1 - 2i}$   
 $\frac{12}{5} - \frac{1}{5}i$

9. Solve by factoring  $x^2 - 4x - 32 = 0$   
 $x = -4, 8$

10. Solve by extracting square roots  $(3x - 1)^2 - 16 = 0$

First you have to have  $(3x - 1)^2$  isolated on one side of the equation:  $(3x - 1)^2 = 16$

You now take the square root of each side and insert  $\pm$ . Essentially you are using the property that if  $a^2 = 16$  then  $a = \pm 4$ .

$$3x - 1 = \pm 4$$

You now solve for  $x$ .

$$3x = 1 \pm 4$$

$$x = \frac{1 \pm 4}{3}$$

When you get an answer of this form that does not involve a radical then you write the separate solutions:

$$x = \frac{1 - 4}{3}, \frac{1 + 4}{3}$$

$$x = -1, \frac{5}{3}$$

11. Solve using the quadratic formula  $2x^2 - 7 = -6x$

$$x = \frac{-3 \pm \sqrt{23}}{2}$$

12. Solve using the quadratic formula  $x^2 + 4x + 13 = 0$

$$x = -2 \pm 3i$$

13. Solve using the quadratic formula  $4x^2 + 25 = 20x$

$$x = \frac{5}{2}$$

14. Solve  $x^4 - x^2 - 20 = 0$

First note that  $(x^2)^2 = x^4$ , making the equation  $(x^2)^2 - x^2 - 20 = 0$

If you put  $a$  in place of  $x^2$ :  $a^2 - a - 20 = 0$

You can now solve this by factoring

$$(a-5)a+4=0$$

$$a=5,-4$$

Since we put  $a$  in place of  $x^2$  we now have

$$x^2 = 5 \text{ or } x^2 = -4$$

You now take the square root of each side and insert  $\pm$ . Remember that the square root of a negative number is imaginary.

$$x = \pm\sqrt{5}, \pm 2i$$

15. Solve  $6\left(\frac{t}{t+2}\right)^2 - 13\left(\frac{t}{t+2}\right) + 6 = 0$ . Hint  $6a^2 - 13a + 6 = (2a-3)(3a-2)$   
 $t = -6, 4$

16. Solve  $\sqrt{5x-26} = x-4$

$$x = 6, 7 \text{ (Both answers check)}$$

17. Solve  $\frac{6}{x+2} - \frac{5}{x+4} = 1$

$$x = 1, -6 \text{ (Both answers check)}$$